



**PARVATHANENI BRAHMAYYA
SIDDHARTHA COLLEGE OF ARTS & SCIENCE**

Autonomous

Siddhartha Nagar, Vijayawada-520010

Re-accredited at 'A+' by the NAAC

23MAVAL101: ELEMENTARY NUMBER THEORY

Offered to: ALL UG PROGRAMS

Course Type: Value Added Course

Semester: I

45 Hours

Credits: 2

Objectives: To enhance the computational skills and application skills.

Unit-I: DIVISIBILITY

15 periods

- 1.1 Introduction and basic properties
- 1.2 Well-Ordering principle, Definition of Divisors
- 1.3 Division algorithm and related problems
- 1.4 GCD, Euclidean Algorithm, problems

Unit -II: PRIMES

15 periods

- 2.1 Relatively prime definition, Euclid's Lemma and Fundamental theorem of Arithmetics
- 2.2 The number of divisors of a positive integer N
- 2.3 Highest power of a prime number containing $n!$ Problems
- 2.4 Bracket function

Unit-III: CONGRUENCES

15 periods

- 3.1 Congruence mod m definition
- 3.2 Congruence classes, linear congruence definition, examples, theorems, problems
- 3.3 Inverse mod m
- 3.4 Euler's ϕ function definition and theorems
- 3.5 Fermat's little theorem and Wilson's theorem

STUDENT ACTIVITIES:

1. Classroom activities: Powerpoint presentations, Assignments
2. Library activities: Visit to library and preparation of notes for assignment problems
3. Activities in the seminars, workshops and conferences: Participation / presentation in Seminars/workshops/conferences

CO-CURRICULAR ACTIVITIES:

- Quiz competitions, seminars, Group discussions

Text Book: A text book of Mathematics B.A/B.Sc Vol- 1, V.Venkateswararao N.Krishna Murthy BVSS Sharma & S.Anjaneya Sasthry, S.Chand & Co.Ltd, 1988

Reference books: A text book of Mathematics Vol- 1, A.Anjaneyulu, Deepthi Publications, 1988

Question Paper Pattern:

- (a) Continuous Assessment: 15 Marks
(b) Semester End Exam: 35 Marks

SEE Consists of two sections-

(i) Section A: Set 5 questions, at least one question from each unit answer any Three out of 5 questions. Each question carries 5 Marks ($5M \times 3 = 15$)

(ii) Section B: Set 3 questions, one from each unit. Each question carries 10 Marks ($10M \times 2 = 20$)

MODEL QUESTION PAPER

23MAVAL101: ELEMENTARY NUMBER THEORY

SEMESTER –I

Max. Marks: 35M

Max.Time: 2Hours

SECTION – A

Answer any THREE of the following

3x5=15 Marks.

1. Prove that every odd integer is of the form $4n+1$ or $4n-1$
2. If $a, b \in \mathbb{Z}, b \neq 0$ and $a = bq + r, 0 \leq r < |b|$ then Prove that $(a, b) = (b, r)$.
3. State and Prove Euclid's Lemma.
4. Find the highest power of 5 in $80!$.
5. Find the number of positive integers less than 25200 that are prime to 25200.

SECTION – B

Answer any TWO of the following.

2x10 =20 Marks

6. State and Prove Fundamental theorem of arithmetic.
7. If $d = (826, 1890)$ using division algorithm compute d and then express as a linear combination of 826, 1890.
8. State and Prove Wilson's theorem.
