



**PARVATHANENI BRAHMAYYA  
SIDDHARTHA COLLEGE OF ARTS & SCIENCE**

*Autonomous*

Siddhartha Nagar, Vijayawada-520010

*Re-accredited at 'A+' by the NAAC*

**23MAVAL101: ELEMENTARY NUMBER THEORY**

**Offered to:** ALL UG PROGRAMS

Course Type: Value Added Course

Semester: I

45 Hours

Credits: 2

**Objectives:** To enhance the computational skills and application skills.

**Unit-I: DIVISIBILITY**

**15 periods**

- 1.1 Introduction and basic properties
- 1.2 Well-Ordering principle, Definition of Divisors
- 1.3 Division algorithm and related problems
- 1.4 GCD, Euclidean Algorithm, problems

**Unit -II: PRIMES**

**15 periods**

- 2.1 Relatively prime definition, Euclid's Lemma and Fundamental theorem of Arithmetics
- 2.2 The number of divisors of a positive integer  $N$
- 2.3 Highest power of a prime number containing  $n!$  Problems
- 2.4 Bracket function

**Unit-III: CONGRUENCES**

**15 periods**

- 3.1 Congruence modulo definition
- 3.2 Congruence classes, linear congruence definition, examples, theorems, problems
- 3.3 Inverse modulo
- 3.4 Euler's  $\phi$  function definition and theorems
- 3.5 Fermat's little theorem and Wilson's theorem

**STUDENT ACTIVITIES:**

1. Classroom activities: Powerpoint presentations, Assignments
2. Library activities: Visit to library and preparation of notes for assignment problems
3. Activities in the seminars, workshops and conferences: Participation / presentation in Seminars/workshops/conferences

**CO-CURRICULAR ACTIVITIES:**

- Quiz competitions, seminars, Group discussions

Text Book: A text book of Mathematics B.A/B.Sc Vol- 1, V.Venkateswararao N.Krishna Murthy BVSS Sharma & S.Anjaneya Sasthy, S.Chand & Co.Ltd, 1988

Reference books: A text book of Mathematics Vol- 1, A.Anjaneyulu, Deepthi Publications, 1988

**Question Paper Pattern:**

- (a) Continuous Assessment: 15 Marks  
(b) Semester End Exam: 35 Marks

**SEE Consists of two sections-**

**(i) Section A:** Set 5 questions, at least one question from each unit answer any Three out of 5 questions. Each question carries 5 Marks (5M X 3 = 15)

**(ii) Section B:** Set 3 questions, one from each unit. Each question carries 10 Marks (10M X 2 = 20)

**MODEL QUESTION PAPER**

**23MAVAL101: ELEMENTARY NUMBER THEORY**

**SEMESTER –I**

**Max. Marks: 35M**

**Max.Time: 2Hours**

**SECTION – A**

**Answer any THREE of the following**

**3x5=15 Marks.**

1. Prove that every odd integer is of the form  $4n+1$  or  $4n-1$
2. If  $a, b \in \mathbb{Z}, b \neq 0$  and  $a = bq + r, 0 \leq r < |b|$  then Prove that  $(a, b) = (b, r)$ .
3. State and Prove Euclid's Lemma.
4. Find the highest power of 5 in  $80!$ .
5. Find the number of positive integers less than 25200 that are prime to 25200.

**SECTION – B**

**Answer any TWO of the following.**

**2x10 =20 Marks**

6. State and Prove Fundamental theorem of arithmetic.
7. If  $d = (826, 1890)$  using division algorithm compute  $d$  and then express as a linear combination of 826, 1890.
8. State and Prove Wilson's theorem.

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